



FEDERAL PUBLIC SERVICE COMMISSION
COMPETITIVE EXAMINATION FOR
RECRUITMENT TO POSTS IN BS-17
UNDER THE FEDERAL GOVERNMENT, 2015

Roll Number

APPLIED MATHEMATICS, PAPER-I

TIME ALLOWED: THREE HOURS

MAXIMUM MARKS = 100

- NOTE: (i)** Attempt **ONLY FIVE** questions in all, by selecting **THREE** questions from **SECTION-I** and **TWO** questions from **SECTION-II**. **ALL** questions carry **EQUAL** marks.
- (ii)** All the parts (if any) of each Question must be attempted at one place instead of at different places.
- (iii)** Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.
- (iv)** No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
- (v)** Extra attempt of any question or any part of the attempted question will not be considered.
- (vi)** **Use of Calculator is allowed.**

SECTION-I

- Q. No. 1 (a)** Prove that $(\vec{A} + \vec{B}) \cdot (\vec{B} + \vec{C}) \times (\vec{C} + \vec{A}) = 2[\vec{A} \cdot (\vec{B} \times \vec{C})]$. **(10)**
- (b)** If $\vec{A} = (x - 3y)\hat{i} + (y - 2x)\hat{j}$, evaluate $\oint_c \vec{A} \cdot d\vec{r}$ where c is an ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ **(10)**
in the xy - plane traversed in the positive direction.
- Q. No. 2 (a)** Determine the expression for divergence in orthogonal curvilinear coordinates. **(10)**
- (b)** Determine the unit vectors in spherical coordinate system. **(10)**
- Q. No. 3 (a)** A particle moves from rest at a distance “ a ” from a fixed point O where the **(10)**
acceleration at distance x is $m x^{-\frac{5}{3}}$. Show that the time taken to arrive at O is given
by an equation of the form $t = A \frac{a^{\frac{4}{3}}}{\sqrt{m}}$, where A is a number.
- (b)** Three forces P, Q, R acting at a point, are in equilibrium, and the angle between **(10)**
 P and Q is double of the angle between P and R . Prove that $R^2 = Q(Q - P)$.
- Q. No. 4 (a)** AB and AC are similar uniform rods, of length a , smoothly joined at A . BD is a **(10)**
weightless bar, of length b , smoothly joined at B , and fastened at D to a smooth
ring sliding on AC . The system is hung on a small smooth pin at A . Show that the
rod AC makes with the vertical an angle $\tan^{-1} \frac{b}{a + \sqrt{a^2 - b^2}}$.
- (b)** Find the centroid of the arc of the curve $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$ lying in the first quadrant. **(10)**
- Q. No. 5 (a)** A hemispherical shell rests on a rough inclined plane whose angle of friction is **(10)**
 λ . Show that the inclination of the plane base to the horizontal cannot be greater
than $\sin^{-1}(2 \sin \lambda)$.
- (b)** A regular octahedron formed of twelve equal rods, each of weight w , freely **(10)**
jointed together is suspended from one corner. Show that the thrust in each
horizontal rod is $\frac{3}{2}\sqrt{2}w$.

APPLIED MATHEMATICS, PAPER-I

SECTION-II

- Q. No. 6** (a) A particle is moving with uniform speed v along the curve $x^2y = a(x^2 + \frac{a^2}{\sqrt{5}})$. (10)
Show that its acceleration has the maximum value $\frac{10v^2}{9a}$.
- (b) Discuss the motion of a particle moving in a straight line if it starts from rest at a distance a from a point O and moves with an acceleration equal to m times its distance from O . (10)
- Q. No. 7** (a) Prove that the force field (10)
 $F = (y^2 - 2xyz^3)i + (3 + 2xy - x^2y^3)j + (6z^3 - 3x^2yz^2)k$
is conservative, and determine its potential.
- (b) The components of velocity along and perpendicular to the radius vector from a fixed origin are respectively $1/r^2$ and $m\theta^2$. (10)
Find the polar equation of the path of the particle in terms of r and θ .
- Q. No. 8** (a) A particle is projected horizontally from the lowest point of a rough sphere of radius a . After describing an arc less than a quadrant, it returns and comes to rest at the lowest point. Show that the initial speed must be $(\sin \alpha)\sqrt{\frac{2ag(1+m^2)}{(1-2m^2)}}$, (10)
Where m is the coefficient of friction and α is the arc through which the particle moves.
- (b) The law of force is Mu^2 and a particle is projected from or apse at distance a . Find (10)
the orbit when the velocity of the projection is $\frac{\sqrt{M}}{a^2}$.



FEDERAL PUBLIC SERVICE COMMISSION
COMPETITIVE EXAMINATION FOR
RECRUITMENT TO POSTS IN BS-17
UNDER THE FEDERAL GOVERNMENT, 2015

Roll Number

APPLIED MATHEMATICS, PAPER-II

TIME ALLOWED:
THREE HOURS

MAXIMUM MARKS: 100

- NOTE:(i)** Attempt **FIVE** questions in all by selecting **TWO** questions from **SECTION-A**, **ONE** question from **SECTION-B** and **TWO** questions from **SECTION-C**. **ALL** questions carry **EQUAL** marks.
- (ii)** Candidate must write **Q.No.** in the **Answer Book** in accordance with **Q.No.** in the **Q.Paper**.
- (iii)** All the parts (if any) of each Question must be attempted at one place instead of at different places.
- (iv)** Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.
- (v)** No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
- (vi)** Extra attempt of any question or any part of the attempted question will not be considered.
- (vii)** **Use of Calculator is allowed.**

SECTION-A

- Q. No. 1. (a)** Solve the initial value problem. (10)
$$\frac{dy}{dx} + \frac{y}{2x} = \frac{x}{y^3}, y(1) = 2$$
- (b)** Solve $y'' - 4y' + 4y = e^{2x}$ (10)
- Q. No. 2.** Solve the following equations: (10)
- (a)** $(1 - x^2) \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} + 2y = 0$
- (b)** $\frac{d^3 y}{dx^3} + \frac{dy}{dx} = \operatorname{cosec} x$ (10)
- Q. No. 3. (a)** Classify the following: (5 each) (10)
- (i)** $x^2 U_{xx} + (a^2 - y^2) U_{yy} = 0$, $-\infty < x < \infty, -a < y < a$
- (ii)** $U_{xx} - 6U_{xy} + 9U_{yy} + 3y = 0$
- (b)** Solve (10)
$$\frac{\partial^2 u}{\partial^2 t} = \frac{\partial^2 u}{\partial^2 x} \quad 0 < x < 5$$

$$u(0, t) = u(5, t) = 0$$

$$u(x, 0) = x^2(x - 5)$$

$$u_t(x, 0) = 0$$

SECTION-B

- Q. No. 4. (a)** Prove that if A_i and B_j are two first order tensors, then their product (7)
 $A_i B_j (i, j = 1, 2, 3)$ is a second order tensor.
- (b)** If $f(x_1, x_2, x_3)$ is a scalar point function then $\frac{\partial f}{\partial x_i}$ are the components of a first (7)
order tensor.
- (c)** Find the invariant of the following second order tensor (6)

$$\begin{bmatrix} 2 & 4 & -1 \\ 6 & -7 & 10 \\ 3 & -4 & 6 \end{bmatrix}$$

APPLIED MATHEMATICS, PAPER-II

Q. No. 5. (a) Verify that the transformation (7)

$$\begin{aligned}x_1' &= \frac{1}{15}(5x_1 - 14x_2 + 2x_3) \\x_2' &= -\frac{1}{3}(2x_1 + x_2 + 2x_3) \\x_3' &= \frac{1}{15}(10x_1 + 2x_2 - 11x_3)\end{aligned}$$

Is orthogonal and right handed. A vector field $\vec{A}$ is defined in the system

$$Ox_1x_2x_3 \text{ by } A_1 = x_1^2, A_2 = x_2^2, A_3 = x_3^2$$

Evaluate the components A_j' of the vector field in the new system $Ox_1'x_2'x_3'$.

(b) Prove that any second order tensor A_{ij} can be written as the sum of a deviator and an isotropic tensor. (7)

(c) If $a_{ij} = a_{ji}$ are constants. Calculate. (6)

$$\frac{\partial^2}{\partial X_k \partial X_m}(a_{ij} X_i X_j)$$

SECTION-C

Q. No. 6. (a) Find the real root of the equation by using Newton – Raphson’s method. (10)
 $3x - \cos x - 1 = 0$

(b) Solve the following system of equations by Gauss-Seidel method. (10)
Take initial approximation as $x_1 = 0, x_2 = 0, x_3 = 0$. Perform 3 Iterations.
 $20x_1 + x_2 - 2x_3 = 17$
 $3x_1 + 20x_2 - x_3 = -18$
 $2x_1 - 3x_2 + 20x_3 = 25$

Q. No. 7. (a) Find the real root of the equation $x^3 - 4x - 9 = 0$ by Regular falsi method. Take the interval of the root as (2,3) and perform 4 iterations. . (10)

(b) Find a polynomial which possess through the following points: (10)

$$\begin{array}{ccccc}x: & -1 & 0 & 1 & 2 \\f(x): & 2 & 1 & 2 & 5\end{array}$$

Q. No. 8. (a) Use the langrage’s Interpolation formula to find the value $f(12)$ if the values of x and $f(x)$ are given below (10)

$x:$	5	7	11	13
$f(x)$	150	392	1452	2366

(b) Evaluate $\int_0^3 x\sqrt{1+x^2} dx$ using $\frac{1}{3}$ Simpson’s rule and trapezoidal rule for $n = 6$ (10)
